

# Thesis Defense

On the Performance Analysis over Generalized and Composite  
Fading Channels: A Unified Approach

Omar Alhussein

School of Engineering Science  
Simon Fraser University

August 26, 2015

# Contents

- 1 Introduction
- 2 Objectives and Contributions
- 3 Modeling Fading Channels using the MoG distribution
  - The MoG distribution
  - Approximation Methodology
  - Performance Analysis
- 4 Modeling Fading Channels using the  $MG$  Distribution
  - The  $MG$  Distribution
  - The Approximation Methodology
  - Applications of Mixture Gamma
- 5 Energy Detection over Generalized and Composite Fading Channels
- 6 Analysis of Wireless Systems over Generalized and Composite Fading Channels with Impulsive Noise
- 7 Conclusions and Future Work

## Introductory Background | Fading Channels

This thesis is concerned with providing a **unified approach** to modeling or approximating **wireless fading channels**.

- Large-scale (Shadowing) Effect
  - Lognormal, Inverse-Gaussian, Gamma.

## Introductory Background | Fading Channels

This thesis is concerned with providing a **unified approach** to modeling or approximating **wireless fading channels**.

- Large-scale (Shadowing) Effect
  - Lognormal, Inverse-Gaussian, Gamma.
- Small-scale (Multipath) Effect
  - **Conventional:** Rayleigh, Nakagami- $m$ , Weibull- $m$ , Rician.
  - **Generalized:**  $\alpha - \mu$ ,  $\kappa - \mu$ ,  $\eta - \mu$ .

Screenshot 2015-08-25 23.41.58.]

## Introductory Background | Composite Fading Channels (1)

Performance analysis over multipath or shadowing scenarios alone is relatively tractable. However, extending the analysis to **composite fading** channels is rather **cumbersome** and **intractable**.

- Examples:
  - Nakagami- $m$ /Lognormal (NL) model (**no closed-form**)

$$f_{\gamma}(x) = \frac{2\lambda m^m}{\Gamma(m)\sqrt{2\pi}\zeta} \int_0^{\infty} \frac{x^{m-1}}{\bar{\gamma}^m \sigma^{m+1}} e^{-\frac{mx}{\bar{\gamma}\sigma}} e^{-\frac{(\mathbf{10} \log \sigma)^2}{2\zeta^2}} d\sigma. \quad (1)$$

- $\kappa - \mu$  Shadowed model [1] (**complicated**)

$$f_{\gamma}(\gamma) = \frac{\mu^{\mu} m^m (1 + \kappa)^{\mu}}{\Gamma(\mu) \bar{\gamma} (\mu \kappa + m)^m} \left(\frac{\gamma}{\bar{\gamma}}\right)^{\mu-1} \times \exp\left(-\frac{\mu(1 + \kappa)\gamma}{\bar{\gamma}}\right) {}_1F_1\left(m, \mu; \frac{\mu^2 \kappa (1 + \kappa) \gamma}{\mu \kappa + m} \frac{\gamma}{\bar{\gamma}}\right), \quad (2)$$

[1] J. F. Paris, "Statistical Characterization of  $\kappa$ - $\mu$  Shadowed Fading," IEEE Trans. Veh. Technol., vol. 63, no. 2, pp. 518–526, Feb. 2014.

## Introductory Background | Composite Fading Channels (2)

- Various alternatives proposed, for examples:

## Introductory Background | Composite Fading Channels (2)

- Various alternatives proposed, for examples:
  - The  $K$ - and  $K_G$ - distributions:
    - Replaced the Lognormal with Gamma and integrate.

## Introductory Background | Composite Fading Channels (2)

- Various alternatives proposed, for examples:
  - The  $K$ - and  $K_G$ - distributions:
    - Replaced the Lognormal with Gamma and integrate.
  - The RIGD and  $G$ -distribution:
    - Replaced the Lognormal with Inverse-Gaussian (IG) and integrate.



## Introductory Background | Composite Fading Channels (2)

- Various alternatives proposed, for examples:
  - The  $K$ - and  $K_G$ - distributions:
    - Replaced the Lognormal with Gamma and integrate.
  - The RIGD and  $G$ -distribution:
    - Replaced the Lognormal with Inverse-Gaussian (IG) and integrate.
- Still **complex** and **not** a general solution.

## Introductory Background | Composite Fading Channels (3)

- Another alternative proposed by Atapattu et al. [2]
  - Several models were approximated using the mixture Gamma ( $MG$ ) distribution via gauss-quadrature approximations.
  - Approximates: NL,  $K$ ,  $K_G$ ,  $\eta - \mu$ ,  $\kappa - \mu$ , Hoyt, and Nakagami- $m$ .
- The pdf is given by

$$f_\gamma(\gamma) = \sum_{i=1}^K \frac{\alpha_i}{\bar{\gamma}} \frac{x^{\beta_i-1}}{\bar{\gamma}} \exp\left(-\frac{\zeta_i x}{\bar{\gamma}}\right)$$

## Introductory Background | Composite Fading Channels (3)

- Another alternative proposed by Atapattu et al. [2]
  - Several models were approximated using the mixture Gamma ( $MG$ ) distribution via gauss-quadrature approximations.
  - Approximates: NL,  $K$ ,  $K_G$ ,  $\eta - \mu$ ,  $\kappa - \mu$ , Hoyt, and Nakagami- $m$ .
- The pdf is given by

$$f_{\gamma}(\gamma) = \sum_{i=1}^K \frac{\alpha_i}{\bar{\gamma}} \frac{x^{\beta_i-1}}{\bar{\gamma}} \exp\left(-\frac{\zeta_i x}{\bar{\gamma}}\right)$$

- **Pros:** Very tractable, arbitrarily accurate.
- **Cons:** Still not generalizable to all fading models.

[2] S. Atapattu, C. Tellambura, and H. Jiang, "A Mixture Gamma Distribution to Model the SNR of Wireless Channels," IEEE Trans. Wireless Commun., vol. 10, no. 12, pp. 4193–4203, Dec. 2011.

# Objectives

We propose to approximate generalized and composite fading channels using mixture distributions, namely using the **mixture of Gaussian** (MoG) and **mixture Gamma** ( $MG$ ) distributions.

# Objectives

We propose to approximate generalized and composite fading channels using mixture distributions, namely using the **mixture of Gaussian** (MoG) and **mixture Gamma** ( $MG$ ) distributions.

- Approximation methodologies:
  - **Expectation-Maximization** (EM) and **Variational Bayes** (VB).

# Objectives

We propose to approximate generalized and composite fading channels using mixture distributions, namely using the **mixture of Gaussian** (MoG) and **mixture Gamma** ( $MG$ ) distributions.

- Approximation methodologies:
  - **Expectation-Maximization** (EM) and **Variational Bayes** (VB).
- EM was coined by Dempster *et al.* [3].
  - Useful for finding the maximum likelihood estimator (MLE) of any distribution in the exponential family.

## Objectives

We propose to approximate generalized and composite fading channels using mixture distributions, namely using the **mixture of Gaussian** (MoG) and **mixture Gamma** ( $MG$ ) distributions.

- Approximation methodologies:
  - **Expectation-Maximization** (EM) and **Variational Bayes** (VB).
- EM was coined by Dempster *et al.* [3].
  - Useful for finding the maximum likelihood estimator (MLE) of any distribution in the exponential family.
- VB is the full Bayesian variant of EM; maximize the maximum *a posteriori* (MAP) estimate.

[3] A. P. Dempster, N. M. Laird, and D. B. Rubin, "Maximum likelihood from incomplete data via the EM algorithm," J. Royal Statistical Soc., vol. 39, no. 1, pp. 1–38, 1977.

## The MoG distribution

- We approximate the amplitude of fading models by the MoG distribution, resulting in the following amplitude and signal-to-noise (SNR) pdfs:

### The MoG distribution

$$f_{\alpha}(x) = \sum_{j=1}^C \frac{\omega_j}{\sqrt{2\pi\eta_j}} \exp\left(-\frac{(x - \mu_j)^2}{2\eta_j^2}\right), \quad (3)$$

$$f_{\gamma}(\gamma) = \sum_{j=1}^C \frac{\omega_j}{\sqrt{8\pi\bar{\gamma}\eta_j}} \frac{1}{\sqrt{\gamma}} \exp\left(-\frac{(\sqrt{\frac{\gamma}{\bar{\gamma}}} - \mu_j)^2}{2\eta_j^2}\right), \quad (4)$$

where  $C$  is the number of mixture components, and  $\omega_j$ ,  $\mu_j$ ,  $\eta_j^2$  correspond to the weights, means and variances, respectively.



## Expectation-Maximization

### Original Problem formulation

Assume that an observed vector  $\mathbf{y} = \{y_1, \dots, y_N\}$ , drawn from any of the fading channel amplitudes, follows the MoG distribution. Then we need to find the MLE as follows:

$$\begin{aligned}\theta_{MLE} &= \arg \max_{\theta \in \hat{\Theta}} \mathbb{L}_{(MoG)}(\theta | \mathbf{y}, C) = \arg \max_{\theta \in \hat{\Theta}} \ln p(\mathbf{y} | \theta, C), \\ &= \arg \max_{\theta \in \Theta} \sum_{i=1}^N \ln \left[ \sum_{j=1}^C \frac{\omega_j}{\sqrt{2\pi}\eta_j^2} \exp\left(-\frac{(y_i - \mu_j)^2}{2\eta_j^2}\right) \right].\end{aligned}\quad (5)$$

- Maximization of (5) directly is analytically **not** tractable.
- Instead, the problem is re-formulated such that it fits the EM framework.

## Expectation-Maximization

### Problem re-formulated according to EM

Regard the observed data  $\mathbf{y}$  as **incomplete** and assume that we have a discrete latent random variable called  $Z \in \{1, \dots, C\}$ , such that the complete random variable is  $X = (Y, Z)$ .

Correspondingly, we maximize the complete-data log-likelihood function or the so-called  $\mathbb{Q}$ -function as follows:

$$\begin{aligned}\theta^{(t+1)} &= \arg \max_{\theta \in \Theta} \mathbb{Q}(\theta | \theta^{(t)}) & (6) \\ &= \arg \max_{\theta \in \Theta} \mathbb{E}_{X|y, \theta^{(t)}} [\log p_X(X|\theta)], \\ &= \arg \max_{\theta \in \Theta} \sum_{i=1}^N \sum_{j=1}^C \rho_{ij}^{(t)} (\ln \pi_j - \ln \mathcal{N}(y_i | \mu_j, \sigma_j)),\end{aligned}$$

## Expectation-Maximization

### EM treatment to the MoG distribution

- **E**-step: Compute  $\rho_{ij}^{(t)}$ .
- **M**-step: Compute:

$$\omega_j^{(t+1)} = \frac{1}{N} \sum_{i=1}^N \rho_{ij}^{(t)}, \quad \mu_j^{(t+1)} = \frac{1}{N\omega_j^{(t+1)}} \sum_{i=1}^N \rho_{ij}^{(t)} y_i,$$

$$\eta_j^{(t+1)} = \frac{1}{N\omega_j^{(t+1)}} \sum_{i=1}^N \rho_{ij}^{(t)} \left( y_i - \mu_j^{(t)} \right)^2, \quad j = 1, \dots, C.$$

- This iterative procedure is terminated upon convergence, that is when

$$\mathbb{L}_{(MoG)}^{(t+1)}(\theta|\mathbf{y}, C) - \mathbb{L}_{(MoG)}^{(t)}(\theta|\mathbf{y}, C) < \delta, \quad (7)$$

## Expectation-Maximization

- **Pros:**
  - Accurate *w.r.t.* mean-square error (MSE) and Kullback-Leibler (KL) divergence.
- **Cons:**
  - Still no method to determine the optimal  $C$ .
  - Singularities can occur during simulation due to overfitting.

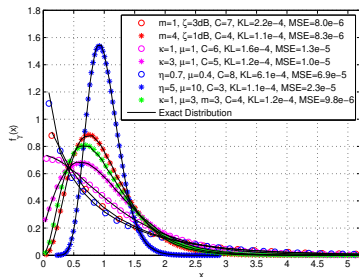


Figure: MoG approximation for different channel models.

## Bayesian Information Criterion for EM

- Bayesian information criterion (BIC) is an information-theoretic method to determine an appropriate number of mixture components.
- Introduced by Gideon Schwarz in 1978 [4].
- Adds a penalty term to the negative log-likelihood as follows:

$$BIC_C = -2\mathbb{L}_{(MoG)}(\hat{\theta}|\mathbf{y}, C) + C \ln N$$

[4] G. Schwarz and Others, "Estimating the dimension of a model," The annals of statistics, vol. 6, no. 2, pp. 461–464, 1978.

# Bayesian Information Criterion for EM

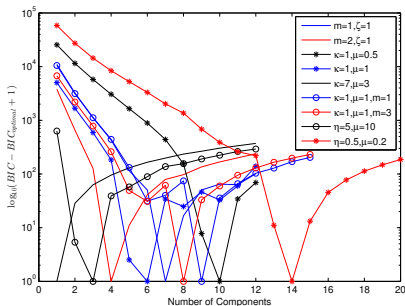


Figure: Normalized BIC versus the number of components

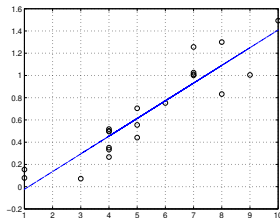


Figure: Optimal number of components versus the amount of fading

## Variational Bayes (VB)

- Variational inference is a bayesian approximation technique that eliminates the challenges:

## Variational Bayes (VB)

- Variational inference is a bayesian approximation technique that eliminates the challenges:
  - Possibility of facing singularities and over-fitting.
  - No effecient method to determine the number of mixture components directly (on-the-go).



## Variational Bayes (VB)

- Variational inference is a bayesian approximation technique that eliminates the challenges:
  - Possibility of facing singularities and over-fitting.
  - No efficient method to determine the number of mixture components directly (on-the-go).
- VB aims to maximize the *a posteriori* rather than the likelihood. Moreover, the parameters to be estimated,  $\theta$ , are treated as nondeterministic (random variables).

# Variational Bayes

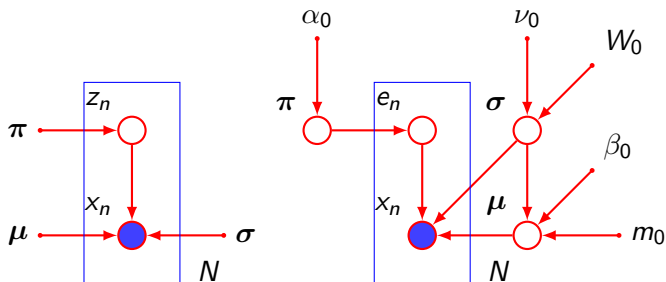


Figure: Bayesian networks representing EM (left) and VB [5] (right).

# Variational Bayes

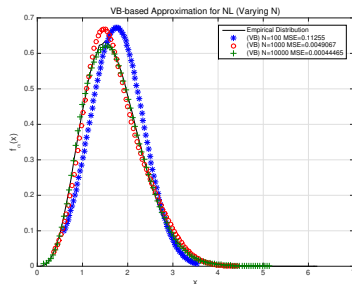
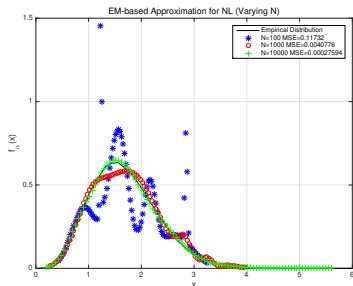


Figure: EM- (left) and VB-based (right) approximations of the NL distribution with  $m = 2$ . The blue, red, and green distributions correspond to  $1E2$ ,  $1E3$ , and  $1E4$  data points with  $C = 6$ .

## Performance Analysis | Intro

To provide simplifying and unifying analysis for wireless communication systems over various generalized and composite fading channel models.

- Moment generating function (MGF).
  - Average Channel Capacity,  $\bar{C}$ .
  - Symbol Error Rate of  $L$ -branch MRC system.
- Raw Moments.
  - Amount of Fading (AoF).
- Outage Probability.

## Performance Analysis | Results

$$M_\gamma(s) = \sum_{i=1}^C \frac{\omega_i}{\sqrt{\beta_i}} \exp\left(\frac{\mu_i^2 s}{\beta_i}\right) Q\left(-\frac{\mu_i}{\eta_i \sqrt{\beta_i}}\right), \quad (8)$$

$$\mathbb{E}[\gamma^n] = \sum_{i=1}^C \omega_i \bar{\gamma}^n \eta_i^{2n} 2^n \frac{\Gamma(n + \frac{1}{2})}{\sqrt{\pi}} {}_1F_1\left[-n, \frac{1}{2}, -\frac{\mu_i^2}{2\eta_i^2}\right], \quad (9)$$

$$\text{AoF} = \frac{\mathbb{E}[\gamma^2] - \mathbb{E}[\gamma]^2}{\mathbb{E}[\gamma]^2}. \quad (10)$$

$$F(\gamma_{th}) = \sum_{i=1}^C \omega_i \left[ Q\left(-\frac{\mu_i}{\eta_i}\right) - Q\left(\frac{\sqrt{\frac{\gamma_{th}}{\bar{\gamma}}} - \mu_i}{\eta_i}\right) \right], \quad (11)$$

## Performance Analysis | Results

$$\bar{C} \approx \frac{B}{\ln 2} \left[ \ln(1 + \mathbb{E}[\gamma]) - \frac{\mathbb{E}[\gamma^2] - \mathbb{E}^2[\gamma]}{2(1 + \mathbb{E}[\gamma])^2} \right], \quad (12)$$

$$P_s(E) = \frac{1}{\pi} \int_0^{\frac{(M-1)\pi}{M}} \prod_{k=1}^L M_{\gamma_k} \left( \frac{\sin^2(\frac{\pi}{M})}{\sin^2(\theta)} \right) d\theta, \quad (13)$$

## Performance Analysis | Simulation Results

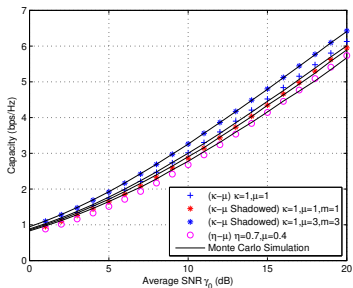


Figure: Analytical and simulated average channel capacity with  $B=\frac{1}{2}$ .

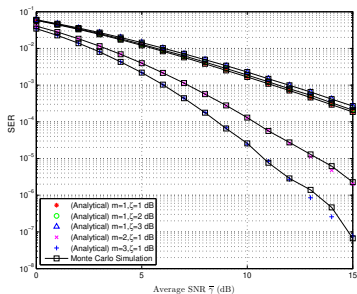


Figure: Analytical and simulation SER of 2-branch MRC receiver with BPSK for NL and RL fading channels.

## The $MG$ Distribution

- Here we approximate the SNRs of fading models by the  $MG$  distribution, resulting in the following:

### The $MG$ distribution

$$f_{\gamma}(x) = \sum_{i=1}^K \frac{\alpha_i}{\bar{\gamma}} \left(\frac{x}{\bar{\gamma}}\right)^{\beta_i-1} \exp\left(-\zeta_i \frac{x}{\bar{\gamma}}\right), \quad (14)$$

where  $K$  denotes the number of mixture components,  $\alpha_i$ ,  $i = 0, \dots, K$ , is the mixing coefficient of the  $i$ th component having the constraints  $0 \leq \frac{\alpha_i \Gamma(\beta_i)}{\zeta_i^{\beta_i}} \leq 1$  and  $\sum_{i=1}^K \frac{\alpha_i \Gamma(\beta_i)}{\zeta_i^{\beta_i}} = 1$ . The scale and shape parameters of the  $i$ th component are  $\beta_i$  and  $\zeta_i$ , respectively.



## Expectation-Maximization

### Original Problem formulation

The observed vector is the SNR, which we call  $\mathbf{x} = \{x_1, \dots, x_N\}$ .

$$\begin{aligned}\theta_{MLE} &= \arg \max_{\theta \in \Theta} \mathbb{L}_{(MG)}(\theta | \mathbf{x}, K) \\ &= \arg \max_{\theta \in \Theta} \sum_{j=1}^N \ln \left[ \sum_{i=1}^K \alpha_i x_j^{\beta_i - 1} \exp(-\zeta_i x_j) \right].\end{aligned}\quad (15)$$

- Unlike in the MoG, the M-step does **not** have closed-form estimates.

# Expectation-Maximization

## EM treatment to the $MG$ distribution

- $\mathbb{E}$ -step: Compute:  $\tau_{ij}^{(t)} = \frac{\alpha_i \phi(x_j | \beta_i, \zeta_i)}{\sum_{l=1}^N \alpha_l \phi(x_j | \beta_l, \zeta_l)}$ .
- $\mathbb{M}$ -step: Compute:  $\alpha_i^{(t+1)} = \frac{1}{N} \sum_{j=1}^N \tau_{ij}^{(t)}$ .
  - As for  $\beta_i, \zeta_i$  coefficients, they are approximated directly using non-linear approximation method, namely Newton-Raphson algorithm.
  -

# Expectation-Maximization | Analysis

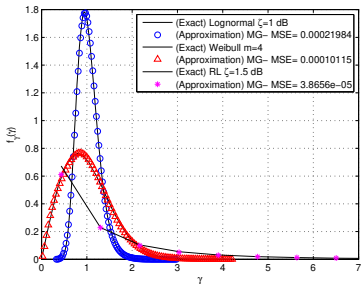


Figure: Approximation of instantaneous SNR distribution of Lognormal, Weibull, and RL for  $M = 0$  dB.

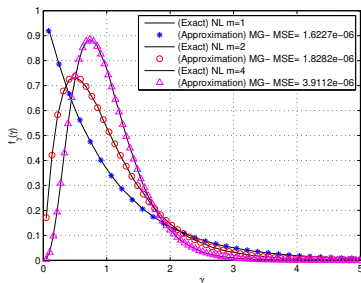


Figure: Approximation of instantaneous SNR distribution of several scenarios of NL distributions for  $M = 0$  dB,  $\zeta = \frac{1}{2}$  dB, with varying  $m$ .

## Fixed-gain dual-hop relaying scenario

- Consider a dual-hop amplify-and-forward (AF) relaying scenario such that

$$\gamma_{end-to-end} = \frac{\gamma_{SR_1} \gamma_{R_1D}}{\gamma_{R_1D} + U},$$

where  $U = \frac{1}{G^2 N_{01}}$  is a fixed-gain constant.

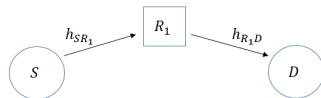


Figure: Fixed-gain dual-hop cooperative communication system.

## Raw Moments

- To calculate the raw moments of composite fading channels in such system is **intricate**. However, with the MG distribution:

$$\mathbb{E}[\gamma^n] = \int_0^\infty \int_0^\infty \left(\frac{\gamma_1 \gamma_2}{U + \gamma_2}\right)^n f_{\gamma_1}(\gamma_1) f_{\gamma_2}(\gamma_2) d\gamma_1 d\gamma_2, \quad (16)$$

$$\mathbb{E}[\gamma^n] = \sum_{j=1}^K \alpha_{1j} \rho^n \frac{\Gamma(n + \beta_{1j})}{\zeta_{1j}^{n + \beta_{1j}}} \sum_{k=1}^K \frac{\alpha_{2k}}{\rho_2^{\beta_{2k}}} \frac{U \zeta_{2k}}{\Gamma(n)} G_{2,1}^{1,2} \left( \begin{matrix} 1, 1 + \beta_{2k} \\ n + \beta_{2k} \end{matrix} \middle| \frac{\rho_2}{U \zeta_{2k}} \right) \quad (17)$$

## Simulation Results | Average Channel Capacity

- Interesting Scenario:  $|h_{SR_1}| \sim$  Weibull distribution with  $m = 4$ , and  $|h_{R_1D}| \sim$  NL distribution with  $(m = 4, \zeta = 2 \text{ dB})$ .

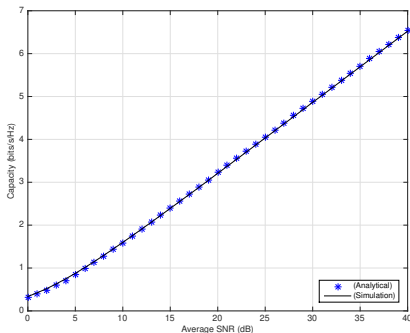


Figure: Average channel capacity for the selected scenario with  $U = 0.5$ , 28 / 39

## Energy Detection Performance

- Cognitive radios came as a viable solution to mitigate the spectrum scarcity.
- Here we are concerned with the performance of the **energy detector** (ED) in generalized and composite fading channels.
  - The literature only offers a semi-analytic solution for the NL.
  - The  $\mathcal{K}$  and  $K_G$  distribution is widely utilized to study the ED performance over RL channels.
- Here we utilize the  $MG$  distribution to study the ED performance.

## Energy Detection Performance

- Goal is to study the detection and false-alarm probabilities in  $MG$ -based fading channels.
- We consider **square-law combining** (SLC) and **square-law selection** (SLS) diversity schemes.
  - We derived the effective effective pdf under SLC,  $f_{\gamma, \Sigma}$ .



## Impulsive Noise | Introduction

- Most of contributions in literature assume white Gaussian noise.
  - Ignoring the impact of impulsive noise caused by atmospheric, man-made partial discharge, switching effect, and electromagnetic interference.

## Impulsive Noise | Introduction

- Most of contributions in literature assume white Gaussian noise.
  - Ignoring the impact of impulsive noise caused by atmospheric, man-made partial discharge, switching effect, and electromagnetic interference.
- Among many models advocated to characterize impulsive noise, we adopt the **Middleton Class-A (MCA)** and  **$\epsilon$ -mixture noise** models.

## Impulsive Noise | Introduction

- Most of contributions in literature assume white Gaussian noise.
  - Ignoring the impact of impulsive noise caused by atmospheric, man-made partial discharge, switching effect, and electromagnetic interference.
- Among many models advocated to characterize impulsive noise, we adopt the **Middleton Class-A (MCA)** and  **$\epsilon$ -mixture noise** models.
- Existing literature: Almost all works on impulsive noise considers multipath fading or shadowing alone.

## MCA and $\epsilon$ -mixture Models

### Middleton's Class-A Model

$$\begin{aligned}
 f_n(x) &= \sum_{k=0}^{\infty} \Pr(T = k) f_{n|T=k}(x|k) \\
 &= \sum_{k=0}^{\infty} \frac{e^{-A} A^k}{k! \sqrt{2\pi\sigma_k^2}} \exp\left(-\frac{x^2}{2\sigma_k^2}\right),
 \end{aligned} \tag{18}$$

where  $A$  is the impulsive index that describes the average number of impulses during some interference time,  $\sigma_k^2 = \frac{kA^{-1} + \Gamma}{1 + \Gamma} \sigma^2$ ,  $\lambda = \frac{\sigma_g^2}{\sigma_i^2}$  is the Gaussian Factor, which resembles the ratio of the variances of the background Gaussian component the impulsive component.

## MCA and $\epsilon$ -mixture Models

### $\epsilon$ -Mixture Model

$$f_n(x) = \frac{1 - \epsilon}{\sqrt{2\pi\sigma_g^2}} \exp\left(-\frac{x^2}{2\sigma_g^2}\right) + \frac{\epsilon}{\sqrt{2\pi\sigma_i^2}} \exp\left(-\frac{x^2}{2\sigma_i^2}\right). \quad (19)$$

where  $\epsilon$  denotes the fraction of time for which the impulsive noise occurs, with  $0 < \epsilon < 1$ . The ratio of the variances of the impulsive component to the Gaussian component is given by  $\xi = \frac{\sigma_i^2}{\sigma_g^2}$ . Here the power of  $n$  is given by  $\sigma^2 = \frac{N_0}{2} = (1 - \epsilon)\sigma_g^2 + \epsilon\sigma_i^2$ .

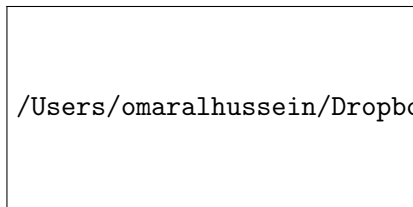
- Note that the truncated two-term MCA model is a subset of the  $\epsilon$ -mixture noise model and not the other way round.

## Performance Analysis

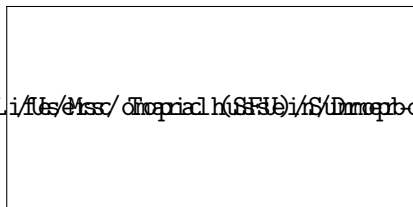
Consider a Single-input-multiple-output communication scenario.

- Again here we consider the  $MG$  distribution.
- We derived the the following:
  - Analytical Pair-wise error probability (**PEP**) expressions with MRC and SC.
  - Analytical Average channel **capacity** expressions with MRC and SC.

## Simulation Results



**Figure:** SEP of BPSK with 4-MRC and 2-SC schemes for various  $MG$  based fading channels with MCA Noise of  $\lambda$ ,  $A = 0.1$ , and  $\dot{C} = 10$ .



**Figure:** SEP of BPSK with MRC scheme for NL fading with MCA Noise of  $\lambda = 0.1$ ,  $A = (0.1, 0.3, 0.9)$ , and  $\dot{C} = 10$ .

## Conclusions

- We represented all generalized and composite fading channels by the MoG and  $MG$  distributions.



## Conclusions

- We represented all generalized and composite fading channels by the MoG and  $MG$  distributions.
- The approximation methodologies relied on MLE and MAP approaches, whereby the EM and VB algorithms were utilized.

## Conclusions

- We represented all generalized and composite fading channels by the MoG and  $MG$  distributions.
- The approximation methodologies relied on MLE and MAP approaches, whereby the EM and VB algorithms were utilized.
- For the MoG distribution, we provided several basic tools essential for the analysis of wireless communication systems.

## Conclusions

- We represented all generalized and composite fading channels by the MoG and  $MG$  distributions.
- The approximation methodologies relied on MLE and MAP approaches, whereby the EM and VB algorithms were utilized.
- For the MoG distribution, we provided several basic tools essential for the analysis of wireless communication systems.
- For the  $MG$  distribution, we nurtured the relevant literature with many contemporary applications, including spectrum sensing, diversity analysis and impulsive noise environments.

## Conclusions

- We represented all generalized and composite fading channels by the MoG and  $MG$  distributions.
- The approximation methodologies relied on MLE and MAP approaches, whereby the EM and VB algorithms were utilized.
- For the MoG distribution, we provided several basic tools essential for the analysis of wireless communication systems.
- For the  $MG$  distribution, we nurtured the relevant literature with many contemporary applications, including spectrum sensing, diversity analysis and impulsive noise environments.

## Future Work

- Several performance analysis tools and applications are yet to be derived.

## Future Work

- Several performance analysis tools and applications are yet to be derived.
- We utilized the vanilla EM and VB frameworks, and advanced variants could be better.

## Future Work

- Several performance analysis tools and applications are yet to be derived.
- We utilized the vanilla EM and VB frameworks, and advanced variants could be better.
- Although our approximation methodology was applied to single fading channels, it can be applied to *fading scenarios*.

## Acknowledgments

- Advisors:
  - Prof. Jie Liang and Prof. Sami Muhaidat.
- Committee:
  - Prof. Paul Ho and Prof. Rodney G. Vaughan.
- Collaborators and Friends:
  - Prof. George Karagiannidis, Prof. Imtiaz Ahmed, Prof. Paschalis Sofotasios, Bassant Selim, Ahmed Al Hammadi, Koos van Nieuwkoop and Xiao Luo.
- Courses:
  - Prof. Ivan Bajic, Prof. Greg Mori, Prof. Faisal Beg, Prof. Paul Ho, and Prof. DanielLee.
- My lab mates, and the school of engineering science..



# Q&A

## Questions and Answers